## Supplementary Data

The usefulness of EM-AMMI to study the influence of missing data pattern and application to Polish post-registration winter wheat data

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Table S1. Analysis of variance for AMMI model based on cell means.

| Source | SS | df | $\mathrm{p}^{\text {c) }}$ |
| :--- | ---: | ---: | ---: |
| $\mathrm{E}^{\text {a) }}$ | 2683.4 | 59 |  |
| G | 79.3 | 23 |  |
| $\mathrm{G} \times \mathrm{E}$ | 450.5 | 1357 |  |
| PC 1 | 125.8 | 81 | 0.0000 |
| PC 2 | 42.4 | 79 | 0.0000 |
| PC 3 | 40.4 | 77 | 0.0000 |
| PC 4 | 34.1 | 75 | 0.0000 |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| PC 16 | 6.4 | 51 | 0.0010 |
| residual | 6.1 | 49 | 0.0652 |
| appr. pooled error ${ }^{\text {b }}$ | 168.5 | 2125 |  |

a) Environment (E) is the combination of Locations and Years
b) The approximated pooled error was calculated based on original trials (based on yields of all cultivars before choosing a complete subset)
c) $p$ was calculated according Cornelius $F_{R}$ test (Cornelius 1993)

Table S2. ANOVA table for three-factor mixed model $\mathrm{G} \times \mathrm{L} \times \mathrm{Y}$

|  | df | SS | F | p |
| :--- | ---: | ---: | ---: | ---: |
| G | 23 | 158.6 | 2.56 | 0.0033 |
| L | 19 | 2517.2 | 3.06 | 0.0016 |
| Y | 2 | 1205.2 | 3799.17 | 0.0000 |
| $\mathrm{G} \times \mathrm{L}$ | 437 | 310.2 | 1.33 | 0.0002 |
| $\mathrm{G} \times \mathrm{Y}$ | 46 | 123.9 | 16.98 | 0.0000 |
| $\mathrm{~L} \times \mathrm{Y}$ | 38 | 1644.5 | 272.84 | 0.0000 |
| $\mathrm{G} \times \mathrm{L} \times \mathrm{Y}$ | 874 | 466.9 | 3.37 | 0.0000 |
| appr. pooled terror ${ }^{\text {a) }}$ | 2125 | 337.1 |  |  |

[^0]Table S3. ANOVA tables for the RMSPD regarding each number of principal components, considering the proportion of missing cells (MProp) and the pattern of missing cells (MPtype) as factors. The SS was obtained according to type III.

| Source of variance | SS | df | MS | F | p |
| :--- | :--- | :--- | :--- | :--- | :--- |
| PC $=0$ |  |  |  |  |  |
| Intercept | 15852896 | 1 | 15852896.4 | 46002011.0 | $<0.001$ |
| MProp | 4734 | 10 | 473.4 | 1373.6 | $<0.001$ |
| MPtype | 65 | 3 | 21.7 | 62.9 | $<0.001$ |
| MProp $\times$ MPtype | 16 | 30 | 0.5 | 1.6 | 0.026 |
| Error | 151615 | 439956 | 0.3 |  |  |
| PC $=1$ |  |  |  |  |  |
| Intercept | 15251903 | 1 | 15251902.9 | 17777344.5 | $<0.001$ |
| MProp | 109991 | 10 | 10999.1 | 12820.3 | $<0.001$ |
| MPtype | 3157 | 3 | 1052.4 | 1226.6 | $<0.001$ |
| MProp $\times$ MPtype | 8141 | 30 | 271.4 | 316.3 | $<0.001$ |
| Error | 377073 | 439510 | 0.9 |  |  |
| PC $=2$ |  |  |  |  |  |
| Intercept | 37103992 | 1 | 37103992.4 | 1707069.9 | $<0.001$ |
| MProp | 114749 | 10 | 11474.9 | 527.9 | $<0.001$ |
| MPtype | 92745 | 3 | 30915.1 | 1422.3 | $<0.001$ |
| MProp $\times$ MPtype | 55079 | 30 | 1836.0 | 84.5 | $<0.001$ |
| Error | 8383311 | 385697 | 21.7 |  |  |
| PC $=3$ |  |  |  |  |  |
| Intercept | 50072286 | 1 | 50072286.2 | 1910252.2 | $<0.001$ |
| MProp | 189536 | 10 | 18953.6 | 723.1 | $<0.001$ |
| MPtype | 164434 | 3 | 54811.5 | 2091.1 | $<0.001$ |
| MProp $\times$ MPtype | 108773 | 30 | 3625.8 | 138.3 | $<0.001$ |
| Error | 9924092 | 378603 | 26.2 |  |  |


[^0]:    ${ }^{\text {a) }}$ The approximated pooled error was calculated based on original trials (based on yields of all cultivars before choosing a complete subset) Genotypes ( G ) and Locations (L) was treated as fixed factors and Years (Y) as a random factor.

